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Discrepancies in the assessment of CO₂ storage capacity and methane recovery from coal with selected equations of state

Part I. Experimental isotherm calculation

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Abstract. The injection of carbon dioxide into coalbeds to increase methane recovery is an emerging technology which was tested in various pilot installations. Carbon dioxide stored in coalbeds is usually in supercritical state and therefore investigation of supercritical adsorption of this gas on coal is a subject of various studies. In the paper impact of three equations of state i.e. Peng Robinson (PR), Soave-Redlich-Kwong (SRK) and the most accurate Span-Wagner, as a reference, on the calculation of sorption capacity was investigated. Langmuir parameters were calculated on the basis of experimental results of CO₂ volumetric sorption by a Selar Cornish coal sample. It is concluded that the use of cubic equation of state (PR and SRK) for the calculation of supercritical CO₂ sorption on coal gives unreliable results by lowering apparent absolute adsorption in the lower pressure range (< 9 MPa) and unrealistically increasing it at higher pressures.

keywords: enhanced coalbed methane, carbon dioxide sequestration, equation of state, sorption by coal

1. Introduction

Enhanced Coalbed Methane Recovery is a technology that was developed in order to increase extraction of methane from coal seams and at the same time mitigate carbon dioxide emissions (Reeves 2003; Pini et al. 2007; Balan and Gumrah 2009). Pilot installations with stimulation of methane recovery by CO₂ injection have been already tested all over the World e.g. Ishikari Coal Basin in Japan (Fujioka et al. 2010), RECOPOL project in Poland (Pagnier et al. 2005), Big Fenn Valley in Canada (Mavor et al. 2004), San Juan Basin in USA (Reeves 2002). An increase of methane production from coal by ECBM technologies is obtained due to a higher affinity of CO₂ to coal resulting in displacement of methane. Once CO₂ is injected, it is permanently trapped as a dense gas in coal cleats and adsorbed on and in coal matrix.

In Europe, coalbeds saturated with methane are located below 750 meters (i.e. where pressure is above 7.5 MPa) and have temperature above 40°C. Therefore, injected CO₂ is under supercritical conditions. Not only storage capacity is an important issue but in order to consider coalbed as suitable for ECBM, the following parameters have to be assessed (Katyal et al. 2007): *P*, *T* and depth of coalbed; coalbed characteristic; type, rank, thickness of coal; mineral matter; moisture content; multi-component sorption/desorption, exchange ratio; coal matrix swelling/shrinkage during adsorption/desorption; cleat permeability and porosity.

Extensive laboratory experiments and geological survey are conducted to obtain all of the above parameters. Later, reservoir simulators are used to incorporate all the abovementioned parameters in order to give an overview of anticipated gas injection/production rates with time. One of the key parameters in ECBM is CO₂ adsorption capacity which is measured in laboratory. Such analyses are performed with the use of either manometric or gravimetric setups (Gensterblum et al. 2009; Li et al. 2010; Pini et al. 2010). On the basis of lab data sorption models such as Langmuir isotherm, BET or Dubinin-Raduschkevich are fit (Ottiger et al. 2006; Sakurovs et al. 2007; Dutta et al. 2008). Accuracy of measurements can have a significant impact on derived parameters of these models. Calculated model parameters are later key input data for reservoir simulators.

In this study, we investigate the impact of equation of state (EoS) on the Langmuir parameters calculated from the same raw laboratory data.

2. Experimental approach

2.1. Sample preparation

Table 1. Properties of U.K Selar Cornish coal used for the experiments

Proximate analysis ¹				
Moisture, wt%	Volatile matter, wt%	Fixed Carbon, wt%	Ash, wt%	
0.64±0.04	9.61±0.02	85.37±0.01	4.38±0.06	
Ultimate analysis ¹				
Carbon, wt%	Hydrogen, wt%	Nitrogen, wt%	Sulfur, wt%	Oxygen, wt%
85.2±1.3	3.28±0.03	0.77±0.05	0.92±0.01	5.60±0.01
Microscope analysis				
R _{max} , %	Vitrinite, vol%	Liptinite, vol%	Inertinite, vol%	Minerals, vol%
2.41	73.6	24.6	0	1.8

¹ Standard deviations reflect the variability of coal from one block used for the experiments. These values are larger for the entire coal layer

Experiments were performed on a semi-anthracite coal sample from a Selar Cornish, South Wales Coalfield. Properties of the coal are presented in Table 1. Coal used for experiments was crushed and sieved to fractions between 1.5 and 2.0 mm. Batches of 50 to 70 cm³ were sealed and stored at temperature of approximately 276 K until the start of experiments. Before the experiment, the sample is evacuated at 322 K for 24 hours in order to remove moisture content. After evacuation the sample is weighted and placed in the cell and experiments are started.

2.2. Experimental setup and procedure

For the purpose of the study highly accurate manometric apparatus was used (Van Hemert et al. 2009). The setup consists of 5 stainless steel cells: two sample cells, two reference cells and one reservoir. Simplified scheme of the setup is presented in Fig. 1. Pressures are measured using highly accurate pressure transducers PTX611 manufactured by DRUCK (+/- 0.001% F.S). In order to keep the temperature of the experiments constant the entire setup is immersed in water bath. Temperature of the experiments is monitored using a PT100 sensor manufactured by Automated System Laboratories. The pressure and temperature sensors are connected to a data acquisition system recording data every 10 seconds.

Before starting the experiment the setup leak-proof was tested by pressurizing He at approximately 20 MPa for more than 25 hours. After the leak test, void volume of the sample cell was determined by He expansion method, with the assumption that He does not adsorb on coal.

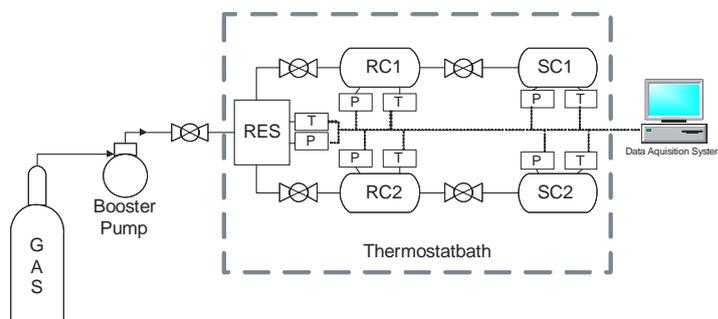


Fig. 1. Scheme of manometric sorption setup used in a study. RES is the reservoir. RC1 and RC2 are reference cells, SC1 and SC2 are sample cells, P and T are pressure transducers and thermocouples respectively

The measuring procedure consists of decompressing known volume of the gas from the reference cell (RC) to the sample cell (SC) under constant temperature. Process of physical adsorption removes adsorbate gas molecules from the free phase to adsorbed phase resulting in decrease in free gas pressure within the system. The total number of moles adsorbed during each pressure step is the difference between the total amount of gas introduced into the void volume of the sample cell and the

amount of free gas occupying the void volume. Repeating this procedure in consecutive steps enables to establish an adsorption isotherm i.e. relation between gas pressure and amount of gas adsorbed under constant temperature.

Physical adsorption of gases in coal is a relatively long lasting process and in order to establish an adsorption isotherm proper equilibration times are needed. In case of carbon dioxide each pressure step may last for up to two weeks whereas for methane up to 10 days. For technical reasons equilibration time at each step was reduced to approximately 48 hours which is in agreement with other publications (Fitzgerald et al. 2005; Prusty 2008; Majewska et al. 2009).

3. Data analysis

In order to obtain adsorption isotherm it is necessary to use equation of state (EoS) for the calculation of gas density. Void volume of the sample was calculated with the use of He EoS published by McCarty (McCarty and Arp 1990). Methane sorption values were calculated using Wagner and Span EoS (Wagner and Span 1993). Carbon dioxide densities were calculated with the use of the following equations of state:

- Peng-Robinson (PR) (Peng and Robinson 1976) and Soave Redlich Kwong (SRK) (Soave 1972) – two cubic equations of state commonly used for carbon dioxide property calculation,
- Span & Wagner (SW) – recently developed accurate equation of state which accuracy up to 523 K and pressure up to 30 MPa ranges from $\pm 0.03\%$ to $\pm 0.05\%$ in the density (Span and Wagner 1996).

Figure 2 shows the carbon dioxide density at 318.15 K computed by three equations of states used in a study. It is clear that the difference in density between reference EoS (i.e. SW) and PR and SRK is much bigger in critical region i.e. above ≈ 7.3 MPa. The relative deviations of SRK and PR from the reference EoS are presented in Fig. 3. Maximum negative deviation is almost 20% in case of SRK and 10% in the pressure region of 10.0-11.0 MPa. Positive deviations are almost 3% for PR near the critical point.

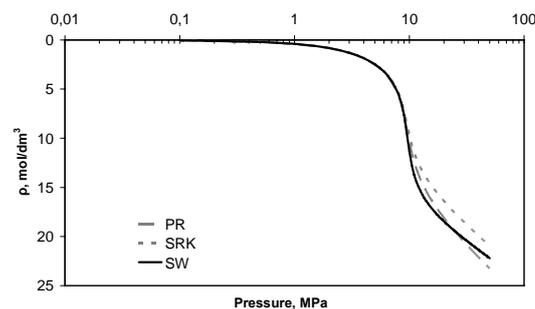


Fig. 2. Density of carbon dioxide (ρ) calculated with three equations of state used in a study (i.e. PR, SRK and SW) at 318.15 K

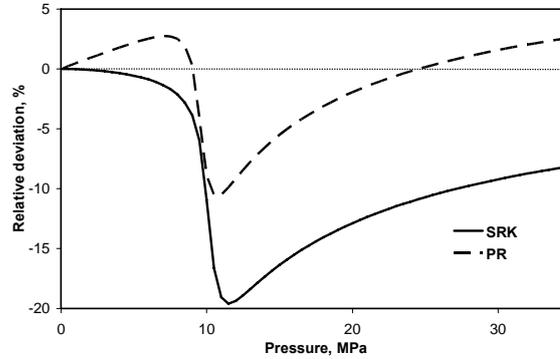


Fig. 3. Relative deviations of SRK and PR for carbon dioxide densities calculated at 318.15 K

Density of carbon dioxide ρ (in mol/m³) is calculated as a function of P [MPa] and T [K] by EoS. The following formula was used for calculation of excess sorption m^N [mol/kg] for measurement N:

$$m^N = \frac{V_{ref}}{M} \left[\sum_{i=1}^N (\rho_{fill}^i - \rho_{eq}^i) - \chi \rho_{eq}^N \right] \quad (1)$$

where the superscript i indicates each sorption step and V_{ref} [cm³] is the volume of the reference cell. M [g] is the mass of the coal sample after evacuation, χ is the volume ratio of the reference cell to the sample cell. Filling and equilibrium stage are denoted by subscripts *fill* and *eq*, respectively.

4. Results and discussion

4.1. Sorption isotherm and Langmuir model fitting

As indicated in the introduction, the purpose of the study was to assess the difference in the calculation of Langmuir parameters based on the isotherm computed with the use of different equations of state. Langmuir parameters are crucial input data in any coalbed methane reservoir simulator and have to be given for an absolute adsorption values in order to represent real gas adsorption of coal. Absolute adsorption can be calculated using the following formula:

$$m^A = m^N \left(\frac{\rho_{ads}}{\rho_{ads} - \rho_{free}} \right), \quad (2)$$

where m^A is the absolute amount of moles adsorbed, m^N is the excess sorption in moles, ρ_{free} and ρ_{ads} is the density of the gas in free and sorbed phase respectively. The density of carbon dioxide in adsorbed phase was calculated by extrapolating experimental data of excess sorption curve on coal to the point where it intersects horizontal axis (i.e. density of free phase reaches the density of sorbed phase) and was assumed to be 42.06 mol/dm³. Such an approach and high values of CO₂ sorbed density were suggested also by other authors (Day et al. 2008; Pini et al. 2009;

Sakurovs et al. 2009), The density of CH₄ sorbed phase was assumed, after Sudibandriyo et al. 2003, to be equal to liquid density (26.41 mol/dm³).

Gas sorption/desorption behaviour on coal is well described by the Langmuir model and indeed it is the most frequently model used in reservoir simulators. The most common form of the Langmuir equation for coalbed methane application is the following:

$$V = \frac{V_L \cdot P}{P_L + P} \quad (3)$$

where V is the volume of gas sorbed per unit mass of coal, V_L is a maximum gas content at infinite pressure (called Langmuir volume) and P_L is the pressure at which half of that gas is in coal (called Langmuir pressure). The Langmuir isotherm model was fitted to experimental data by minimizing the sum of squared residuals with the Excel solver.

In Fig. 4 isotherms calculated with PR, SRK and SW equations of state from the same set of experimental data are presented. It is clear that only in case of SW EoS plotted curve has a shape of type I isotherm (according to IUPAC classification) whereas use of other two equations of state gives erratic results, in particular at pressures above 5 MPa. The reason of these errors lies in the principle of manometric gas sorption measurements and deviations in density calculation by the cubic equations of state. Density of the gas in the Reference Cell calculated by SRK and PR at ~20 MPa is lower in comparison to reference SW EoS (see Fig. 3) but the density at pressures below critical point (i.e. in the Sample Cell) is calculated fairly well. Thus, established isotherm has an apparent lower adsorption at pressures up to critical point. When pressure in the Sample Cell increases above critical region errors in case of PR EoS cancel out to some extent. In case of SRK error at higher pressures is still significant and misrepresents results in the whole range. As it can be seen in Fig. 4 both PR and SRK unrealistically increase calculated sorption capacity above the critical point. The reason for it is again the error in calculated density in the pressure range of approximately 7 – 13 MPa where gas density is significantly lowered with respect to the pressure in the Reference Cell (~20 MPa). This apparently increases calculated adsorption capacity to unrealistic values. In fact, in earlier publications where cubic EoS were used this sudden increase of sorption at higher pressures was visible and could be attributed to the effect explained above (Hall et al. 1994). The above mentioned observations lead to the problem of Langmuir model fitting. Only in the case of SW EoS Langmuir isotherm fitting is satisfactory for the whole range of measured data points. However, gas adsorption on coal is commonly measured in setups which operate within the range of 0-10 MPa. Thus, it was decided to fit Langmuir isotherm model to experimental data of PR calculated points below 10 MPa where the curve has a shape of an isotherm. SRK EoS as far more inaccurate was rejected for further considerations. The calculated Langmuir parameters V_L and P_L for SW are 0.03648 sm³/kg and 0.597 MPa respectively and for PR 0.03071 sm³/kg and 0.406 MPa, respectively. As defined by the ECLIPSE software cubic meter of gas at

standard conditions, that is at 16°C and 1013.25 hPa, per unit mass of coal under *in-situ* conditions is given as sm³/kg.

The deviation in calculated Langmuir parameters V_L and P_L with respect to reference SW EoS is -18.8% and -31.9% respectively.

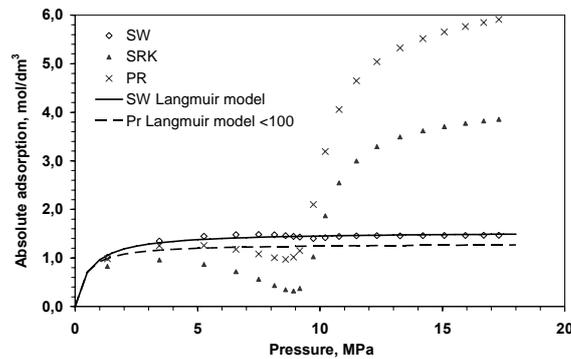


Fig. 4. Absolute adsorption calculated with three equations of state (PR, SRK and SW) and Langmuir model fitting. Note: Langmuir parameters for PR EoS were obtained by fitting experimental points up to 10 MPa

5. Conclusions

From the above study it can be concluded that the use of cubic equation of state (PR and SRK) for the calculation of supercritical CO₂ sorption on coal gives unreliable results by lowering apparent absolute adsorption in the lower pressure range (< 9 MPa) and unrealistically increasing at higher pressures. Fitting the Langmuir model into data calculated with PR is only possible for data points below ~10 MPa and lowers both Langmuir parameters (V_L and P_L). In case of data calculated with SRK EoS it is impossible to fit Langmuir model. In order to assess the impact of these deviations a sensitivity study with the use of reservoir simulator is needed and will be performed in the future.

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Lutynski, M.A., Battistutta, E., Bruining, H., Wolf, K.A.A., Rozbieżności w ocenie ilości składowanego CO₂ i odzysku metanu z pokładu węgla jako wynik zastosowania wybranych równań stanu gazu. Część I. Wyznaczanie izotermy, *Physicochem. Probl. Miner. Process.*, 47 (2011) 159-168, (w jęz. ang.)

Intensyfikacja wydobycia metanu z pokładu węgla za pomocą zatłaczania dwutlenku węgla jest technologią, która nie tylko przyczynia się do zwiększenia uzysku tego surowca energetycznego ale jednocześnie zmniejsza emisję CO₂. Obecnie na Świecie istnieje kilka instalacji pilotowych, w których ta technologia poddawana jest badaniom. W Europie pokłady węglowe bogate w metan występują zazwyczaj na głębokościach przekraczających 750 m i temperaturach powyżej 40°C, a więc w warunkach, w których CO₂ jest w stanie krytycznym. Adsorpcja tego gazu w stanie krytycznym na węglach jest obecnie przedmiotem intensywnych badań. Do wyznaczonych w laboratorium izoterm sorpcji dopasowywane są następnie modele sorpcyjne jak np. izoterma Langmuira, izoterma BET czy model Dubinina-Raduszkiewicza. W pracy przedstawiono wyniki badań sorpcji dwutlenku węgla na węglu antracytowym Selar Cornish z zagłębia Południowej Walii (Wielka Brytania). Do analiz wyników użyto trzech równań stanu gazu stosowanych do określenia gęstości CO₂ tj. równania Penga-Robinsowa (PR), równania Soave-Redlicha-Kwonga (SRK) oraz bardzo dokładnego równania stanu gazu dla CO₂

Spana i Wagnera (SW), jako równania referencyjnego. Do uzyskanych danych sorpcji całkowitej dopasowano model izotermy Langmuira jako powszechnie stosowany w symulatorach złożowych. Obliczone parametry izotermy Langmuira tj. VL oraz PL w przypadku równania SW wyniosły odpowiednio $0.03648 \text{ sm}^3/\text{kg}$ oraz $0,597 \text{ MPa}$, natomiast dla równania PR wartości te wyniosły odpowiednio $0.03071 \text{ sm}^3/\text{kg}$ oraz $0,406 \text{ MPa}$. Odchyłka w obliczonych parametrach w stosunku do równania referencyjnego dla tej samej izotermy wyniosła odpowiednio $-18,8\%$ oraz $-31,9\%$

słowa kluczowe: intensyfikacja wydobycia metanu, sekwestracja dwutlenku węgla, równanie stanu gazu, sorpcja na węglu